

**ECE 281**  
**Electrical Circuits and Instrumentation + Laboratory**  
**Fall 2016/2017**  
**LAB # 6**

7.11.2016

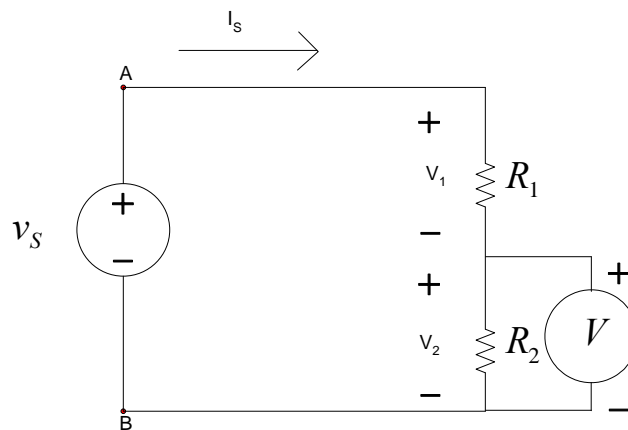
**Objective:**

1. To observe the loading effect of analog voltmeter
  2. To study wheatstone bridge and its properties
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**1. To observe the loading effect of analog voltmeter (15 Points)**

**Procedure:**

1. Construct the circuit given in Figure 1



**Figure 1**

2. First use analog multimeter and measure voltage  $V_2$  for each resistance value, and fill Table 1, Column 3.
3. Use digital multimeter and make the same measurements, and fill Table 1, Column 4.
4. Analyze the circuit to calculate the actual voltage drop  $V_2$  and fill Table 1, Column 5.

$R_1$	$R_2$	$V_2$ (Analog)	$V_2$ (Digital)	$V_2$ (Calculated)
1 k $\Omega$	1 k $\Omega$			
10 k $\Omega$	10 k $\Omega$			
100 k $\Omega$	100 k $\Omega$			
1 M $\Omega$	1 M $\Omega$			
10 M $\Omega$	10 M $\Omega$			
1 k $\Omega$	10 k $\Omega$			

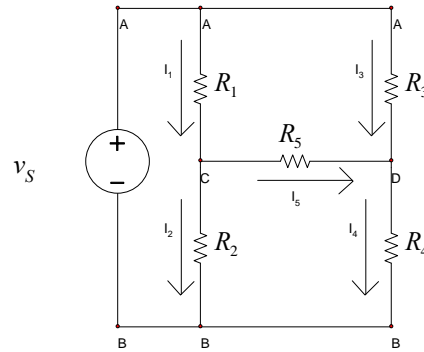
**Table 1**

**Questions:**

- How can we understand that the digital multimeter has higher internal resistance compared to analog multimeter?
- Which multimeter is more accurate in terms of resistance measurements?

## 2. To study Wheatstone bridge and its properties (15 Points)

**Wheatstone bridge:** Wheatstone bridge is a particular circuit which is used to measure unidentified resistance values. In order to figure out the functionality of this particular circuit, let's consider the circuit diagram shown in Figure 4. In this circuit there are five resistors. If no current is observed over the resistor  $R_5$  ( $I_5=0$  A), then this circuit is said to be in **balance condition**. What condition should be satisfied such that the Wheatstone bridge is balance?



**Figure 2:** Wheatstone bridge circuit.

It is seen obvious that

$$I_1 = I_2 + I_5 \quad (1)$$

and

$$I_4 = I_3 + I_5 \quad (2)$$

If  $I_5 = 0$  A (if the Wheatstone bridge is balanced),

$$I_1 = I_2 \quad (3)$$

and

$$I_4 = I_3 \quad (4)$$

Using (3) and (4) and applying node voltage method, we can write,

$$\frac{A-C}{R_1} = \frac{C-B}{R_2} \quad (5)$$

and

$$\frac{A-D}{R_3} = \frac{C-B}{R_4} \quad (6)$$

Again using node voltage method we can also write,

$$C = D + R_5 I_5 \quad (7)$$

As  $I_5 = 0$  A, (7) can be simplified and we can obtain the relation

$$C = D \quad (8)$$

Using (8) inside (6), we can obtain

$$\frac{A-C}{R_3} = \frac{C-B}{R_4} \quad (9)$$

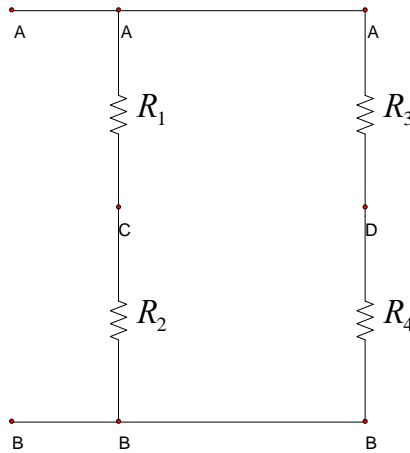
Now using (5) and (9), we can write

$$\frac{R_1}{R_2} = \frac{R_3}{R_4} \quad (10)$$

So the relation shown at (10) should be satisfied for balance condition.

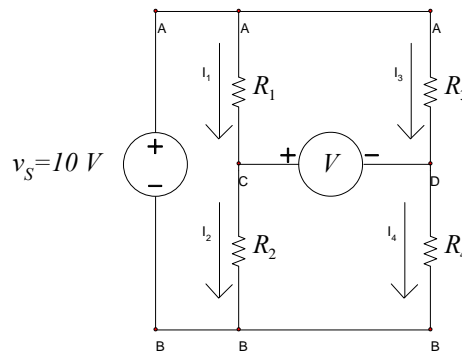
**Procedure:**

1. Use first  $R_1, R_2, R_3,$  and  $R_4$  value combination given in Table 2 and construct the circuit given in Figure 3



**Figure 3**

2. Use digital multimeter, measure resistance between A-B without power.
3. Connect 10V between A-B as shown in Figure 4 and measure the voltage drop between C-D.



**Figure 4**

4. Remove power
5. Repeat steps 1-4 for each Resistor combination given in Table 2, and fill the blanks.

$R_1$	$R_2$	$R_3$	$R_4$	$R_t$ (Between A-B)	V (Between C-D)
1 k $\Omega$	1 k $\Omega$	1 k $\Omega$	1 k $\Omega$		
1 k $\Omega$	10 k $\Omega$	1 k $\Omega$	10 k $\Omega$		
1 k $\Omega$	1 k $\Omega$	10 k $\Omega$	10 k $\Omega$		
1 k $\Omega$	10 k $\Omega$	10 k $\Omega$	1 k $\Omega$		

**Table 2**

**Questions:**

- What is the total resistance if all the resistors have same value?
- When is the voltage is zero (or near to zero) between points C-D?